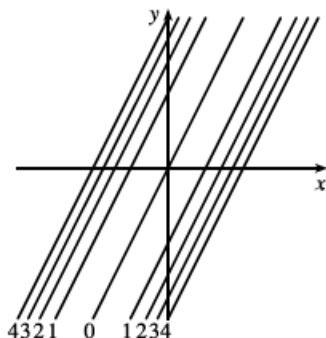


34.

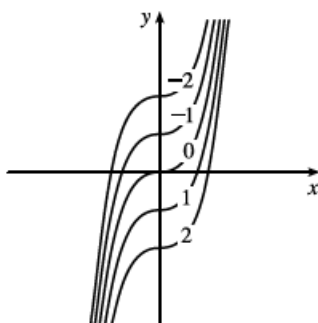
(a)  $C$  (Chicago) lies between level curves with pressures 1012 and 1016 mb, and since  $C$  appears to be located about one-fourth the distance from the 1012 mb isobar to the 1016 mb isobar, we estimate the pressure at Chicago to be about 1013 mb.  $N$  lies very close to a level curve with pressure 1012 mb so we estimate the pressure at Nashville to be approximately 1012 mb.  $S$  appears to be just about halfway between level curves with pressures 1008 and 1012 mb, so we estimate the pressure at San Francisco to be about 1010 mb.  $V$  lies close to a level curve with pressure 1016 mb but we can't see a level curve to its left so it is more difficult to make an accurate estimate. There are lower pressures to the right of  $V$  and  $V$  is a short distance to the left of the level curve with pressure 1016 mb, so we might estimate that the pressure at Vancouver is about 1017 mb.

(b) Winds are stronger where the isobars are closer together (see Figure 13), and the level curves are closer near  $S$  than at the other locations, so the winds were strongest at San Francisco.

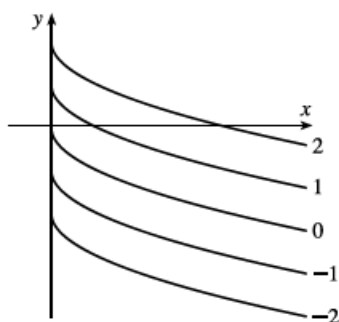
43. The level curves are  $(y - 2x)^2 = k$  or  $y = 2x \pm \sqrt{k}$ ,  $k \geq 0$ , a family of pairs of parallel lines.



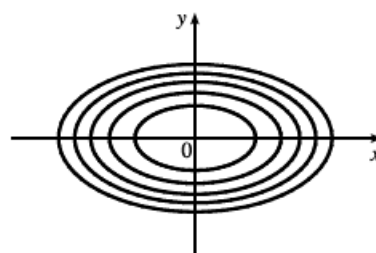
44. The level curves are  $x^3 - y = k$  or  $y = x^3 - k$ , a family of cubic curves.



45. The level curves are  $\sqrt{x} + y = k$  or  $y = -\sqrt{x} + k$ , a family of vertical translations of the graph of the root function  $y = -\sqrt{x}$ .



53. The isothermals are given by  $k = 100/(1 + x^2 + 2y^2)$  or  $x^2 + 2y^2 = (100 - k)/k$  [ $0 < k \leq 100$ ], a family of ellipses.



59.  $z = \sin(xy)$  (a) C (b) II

Reasons: This function is periodic in both  $x$  and  $y$ , and the function is the same when  $x$  is interchanged with  $y$ , so its graph is symmetric about the plane  $y = x$ . In addition, the function is 0 along the  $x$ - and  $y$ -axes. These conditions are satisfied only by C and II.

60.  $z = e^x \cos y$  (a) A (b) IV

Reasons: This function is periodic in  $y$  but not  $x$ , a condition satisfied only by A and IV. Also, note that traces in  $x = k$  are cosine curves with amplitude that increases as  $x$  increases.

61.  $z = \sin(x - y)$  (a) F (b) I

Reasons: This function is periodic in both  $x$  and  $y$  but is constant along the lines  $y = x + k$ , a condition satisfied only by F and I.

62.  $z = \sin x - \sin y$  (a) E (b) III

Reasons: This function is periodic in both  $x$  and  $y$ , but unlike the function in Exercise 61, it is not constant along lines such as  $y = x + \pi$ , so the contour map is III. Also notice that traces in  $y = k$  are vertically shifted copies of the sine wave  $z = \sin x$ , so the graph must be E.

63.  $z = (1 - x^2)(1 - y^2)$       (a) B      (b) VI

Reasons: This function is 0 along the lines  $x = \pm 1$  and  $y = \pm 1$ . The only contour map in which this could occur is VI. Also note that the trace in the  $xz$ -plane is the parabola  $z = 1 - x^2$  and the trace in the  $yz$ -plane is the parabola  $z = 1 - y^2$ , so the graph is B.

64.  $z = \frac{x - y}{1 + x^2 + y^2}$       (a) D      (b) V

Reasons: This function is not periodic, ruling out the graphs in A, C, E, and F. Also, the values of  $z$  approach 0 as we use points farther from the origin. The only graph that shows this behavior is D, which corresponds to V.

65.  $k = x + 3y + 5z$  is a family of parallel planes with normal vector  $\langle 1, 3, 5 \rangle$ .

67. Equations for the level surfaces are  $k = y^2 + z^2$ . For  $k > 0$ , we have a family of circular cylinders with axis the  $x$ -axis and radius  $\sqrt{k}$ . When  $k = 0$  the level surface is the  $x$ -axis. (There are no level surfaces for  $k < 0$ .)